

Phonon Thermal Transport Properties of Graphene Periodically Embedded with Four- and Eight-membered Rings: a Molecular Dynamics Study

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It is studied that the thermal conductivity of graphene periodically embedded with four- and eightmembered rings (GFERs) by using non-equilibrium molecular dynamics simulations. This kind of structure has been experimentally synthesized recently. The dependence of thermal conductivity on the length (L) and temperature (T) is investigated. It is found that the thermal conductivity of GFERs is significantly lower than that of pristine graphene. On the other hand, the length dependence of thermal conductivity follows $\sim \log L$ behavior. In addition, the temperature dependence of thermal conductivity of GFERs follows $\sim T^{-\alpha}$ behavior. It is also found that there exists large thermal rectification (TR) in graphene-GFERs heterostructures, the heat flux from the pristine graphene to the GFERs direction is larger than that in the opposite direction. The dependence of the TR ratio on system parameters is investigated.

Keywords: Thermal conductivity; Thermal rectification; Molecular dynamics simulation; Temperature dependence; Size effect; Four and eight-membered rings

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1. Introduction

Graphene is made of single atomic layer of carbon atoms and forms a two-dimensional honeycomb lattice.¹ As the thinnest two-dimensional material discovered so far, it has excellent thermal, electrical properties, thus attracted enormous interest, since it firstly became experimentally accessible.² Various numerical and theoretical methods have been used to study the lattice thermal conductivity of different graphene structures, among which are the Boltzmann transport equation (BTE) with the relaxation time approximation,³ Monte Carlo (MC) simulations,⁴ and Molecular Dynamics (MD) simulations.^{5–7} MD simulation is a powerful tool to study the thermal properties of nanostructures. Using this approach, thermal conductivity of graphene nanoribbons,^{8–10} graphene phononic crystal,^{11–13} graphene disk,¹⁴ graphene with impurities and defects^{15,16} have been studied. Comparing with pristine graphene, the thermal conductivity of these structures is greatly reduced.

Embedding non-hexagonal rings into sp^2 -hybridized carbon networks is considered a promising strategy to enrich the family of low-dimensional graphene structures. However, non-hexagonal rings are energetically unstable compared to the hexagonal counterparts. Very recently, Liu *et al.*¹⁷ reported on-surface synthesis of graphene-like nanoribbons with periodically embedded four- and eight-membered rings. The thermal transport of this kind of structure has not been considered yet.

Recently, the thermal rectification effect attracts more attentions

due to its vital role in thermal devices¹⁸. The thermal rectification means that the magnitude of heat flux changes when the temperature gradient is reversed in direction. However, it is not easy to obtain a high-performance thermal rectifier. The thermal rectification effect has been found, by theoretical calculations or experimental measurements, in nonlinear lattice models,¹⁹ graded mass density,²⁰ asymmetric structure,^{9,13} quantum system,^{21,22} interfacial structures,²³ or phase change materials^{24,25}. Low dimensional structures tend to realize thermal rectification effect due to ballistic transport of phonons, such as in graphene ribbons⁹ and graphene phononic crystals.¹³

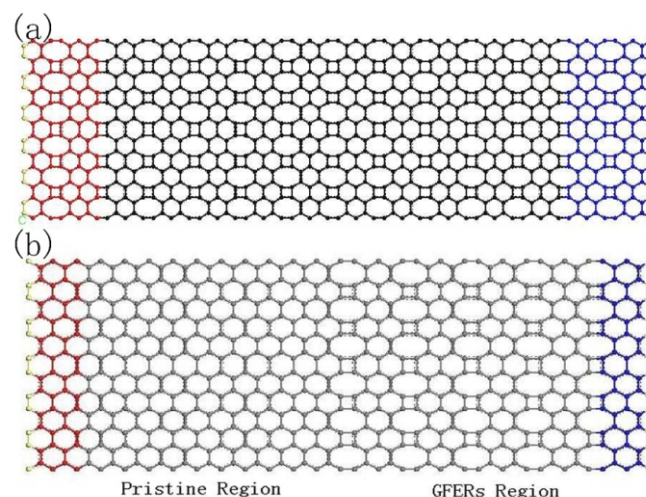


Fig. 1 (a) Schematic picture of GFERs. (b) Schematic picture of graphene-GFERs heterostructure. Periodic boundary condition is used along transverse direction and fixed boundary condition is used in longitudinal direction. Heat bath with higher temperature (red box) T_L and lower temperature (blue box) T_R are applied at two ends.

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In this paper, using non-equilibrium molecular dynamics (NEMD) simulations, the size and temperature dependence of GFERs thermal conductivity have been studied. It is found a drastic drop in the thermal conductivity compared to similar pristine graphene structure. It is also investigated that the thermal rectification property of the graphene-GFERs heterostructure, where the heat flux in one direction is different from that in the opposite direction, and large thermal rectification (TR) ratio is found.

2. Molecular Dynamics Simulation Methods

Fig. 1(a) is a schematic picture of GFERs, and Fig. 1(b) is graphene-GFERs heterostructure where the left region is pristine graphene, and the right region is GFERs. In our calculations, the lattice constant, a , and thickness of graphene are chosen as 1.418 Å and 3.34 Å, respectively. The adaptive intermolecular reactive empirical bond order (AIREBO) potential is used to describe the carbon-carbon interaction, which includes both two-body and three-body potential terms.^{26–28} The fixed (periodic) boundary condition is adopted along the longitudinal (transversal) direction.²⁹ Non-equilibrium MD simulation is performed using LAMMPS³⁰ with the Langevin approach. The equation of motion for the i -th degrees of freedom that couples to the Langevin bath is written as

$$\frac{dp_i}{dt} = \frac{\partial H}{\partial q_i} + \xi_i - \frac{1}{m} \lambda p_i, \quad (1)$$

where H is the Hamiltonian of the system, p_i and q_i are the momentum and coordinate of particle i , λ is the dissipation rate, and ξ_i is the Gaussian random force with zero mean and variance $2m\lambda k_B T$ according to the fluctuation-dissipation theorem. There is a free parameter, λ , which controls the coupling between the system under study and heat bath. For those degrees of freedom that do not couple directly to the baths, the equations of motion do not have the last two terms at the right side of the Eq. (1).^{31,32}

The Langevin equation is integrated by using the velocity Verlet method with a time step of 0.25 fs. The structures are first relaxed at constant temperature, \bar{T} , for 3×10^8 time steps using the Nosé-Hoover thermostat. In order to establish a temperature gradient, the atoms at the two ends are coupled with a Langevin heat bath, whose temperature is $T_L = \bar{T}(1+\Delta)$ in the hot bath, and $T_R = \bar{T}(1-\Delta)$ in cold bath. \bar{T} is average temperature, 2Δ is the relative temperature bias, and steady state is

achieved after 1 ns. The simulation is then continued for another 2 ns for data collection.⁷ The thermal conductivity κ is calculated based on Fourier's Law as^{33,34}

$$\kappa = \frac{J}{Wd(\partial T/\partial x)} \quad (2)$$

where J is the heat flux, which is defined as $J = (dE_{hot}/dt + dE_{cold}/dt)/2$, E_{hot} and E_{cold} are the total energy subtracted from (added by) the hot bath (cold bath), respectively. W is the width of the GFERs, d is the thickness of the sample as 3.34 Å, $\partial T/\partial x$ is the temperature gradient. In order to quantitatively describe the thermal rectification, the TR ratio is defined as

$$\eta = \frac{J_{L \rightarrow R} - J_{R \rightarrow L}}{J_{R \rightarrow L}} \times 100\% \quad (3)$$

where the $J_{L \rightarrow R}$ is the heat flux along the pristine graphene to the GFERs direction, corresponding $\Delta > 0$, $J_{R \rightarrow L}$ is the heat flux along the GFERs to the pristine graphene direction, corresponding $\Delta < 0$.

3. Results and Discussions

Firstly, it is tested that the effect of λ on the calculated κ . To make little effect on the intrinsic properties of the GFERs, λ can not be too large. At the same time, λ can not be too small either. Or else, the time needed to equilibrate the system would be too long, and there will occur a large temperature jump between heat bath and system. Fig. 2(a) shows the results with different λ between 0.01 and 50.0, with other parameters fixed $\bar{T} = 300$ K, $L = 11.67$ nm, $W = 5.2$ nm. It can see that, if λ is too large, the degrees of freedom that couple to the thermal bath can not equilibrate with the baths. As a results, the temperature gradient in the system is small. Consequently, the heat current J_L decreases in Fig. 2(b). This may influence the accuracy of the numerical results. Based on these considerations, an intermediate value of $\lambda = 0.05$ is used for Langevin heat baths.

For the Langevin MD, at two ends of the structure, fixed boundary condition is imposed on the boundary atoms. The heat baths are attached to neighboring atoms.³⁵ But the number of atoms that couple directly to the Langevin bath is a parameter to be chosen. Fig. 3 shows the temperature profile of the structure with different number of atomic layers (NL) attached to the Langevin heat bath. Fig. 4(a) and Fig. 4(b)

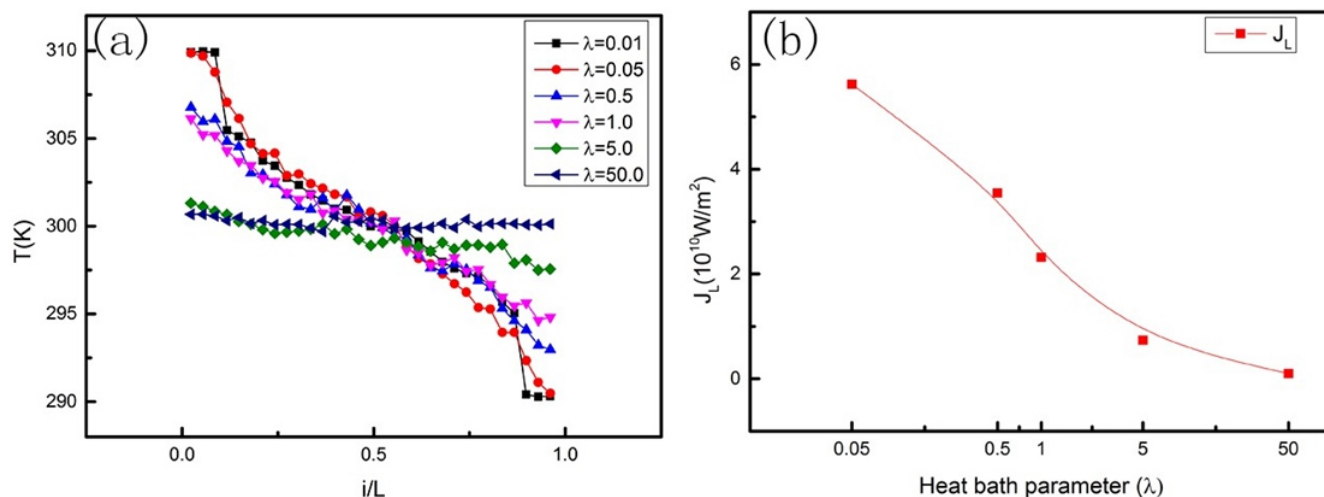


Fig. 2 Impacts of heat bath parameter on thermal properties of GFERs. (a) Temperature profile with parameter λ of Langevin heat bath. (b) Heat flux per cross section area versus λ in logarithmic scale for Langevin heat bath. Here the λ is from 0.01 to 50.0.

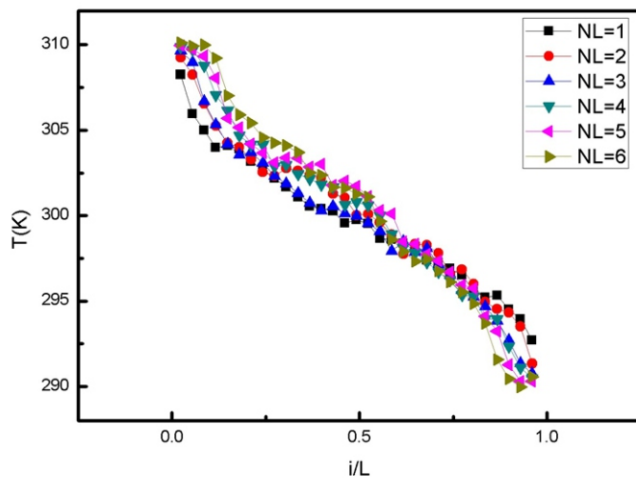


Fig. 3 Temperature profile with different number of layers where the Langevin heat bath is applied.

show the dependence of heat flux per cross section area and the calculated thermal conductivity on NL, respectively. It can be seen that the result converges at $NL = 4$. This is the parameter used in the following calculations.^{36,37}

When the width of simulation cell is not sufficiently large, there will occur a size effect on the thermal conductivity.³⁸ Here, it is studied the dependence of thermal conductivity on the width of the simulation cell. W is changed from 2.6 nm to 7.8 nm. In Fig. 5(a), the results show that with the increase of width, there is little difference between the temperature profile, and the fluctuation gradually becomes smaller when the width is larger.³⁹ The calculated thermal conductivity converges when the width is larger than 5.2 nm in Fig. 5(b). This tendency is consistent with the other study on graphene structure like GNRs,⁴⁰ GPnC,¹² or other graphene structures with defects.⁷ Hence, in the following simulation, GFERS with 5.2 nm in wide are used to eliminate size effect in the transverse direction.⁴¹

After determining the parameters, it is considered that the impact of system length L on the thermal conductivity. Previous study using MD

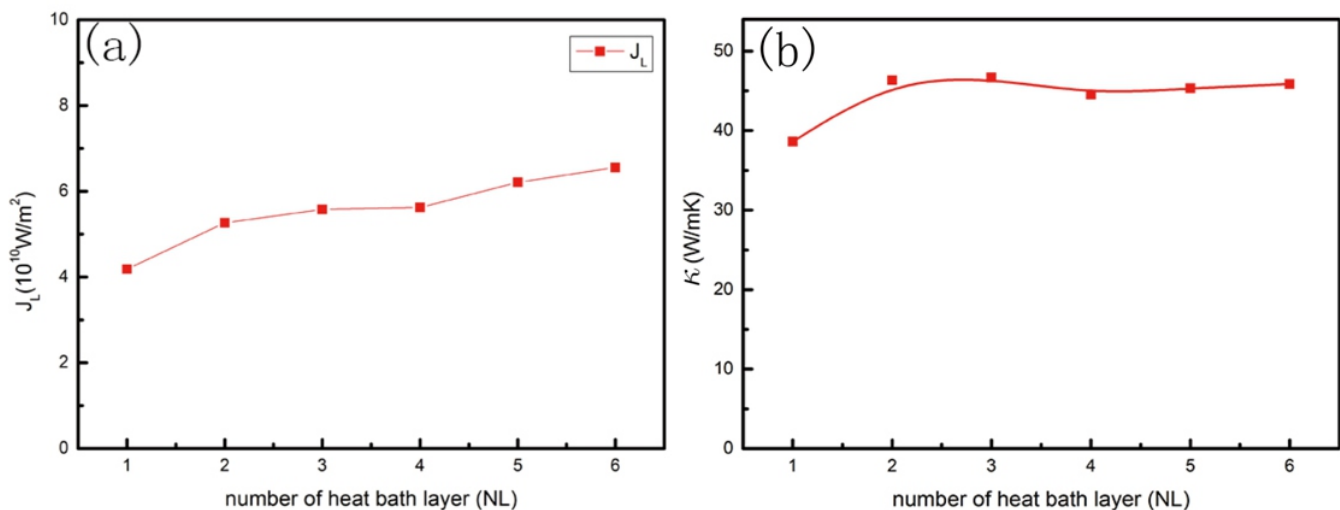


Fig. 4 Impacts of number of heat bath layer on thermal properties of GFERS. (a) Heat flux J_L per cross section area along the longitudinal direction versus NL. (b) Thermal conductivity κ versus NL.

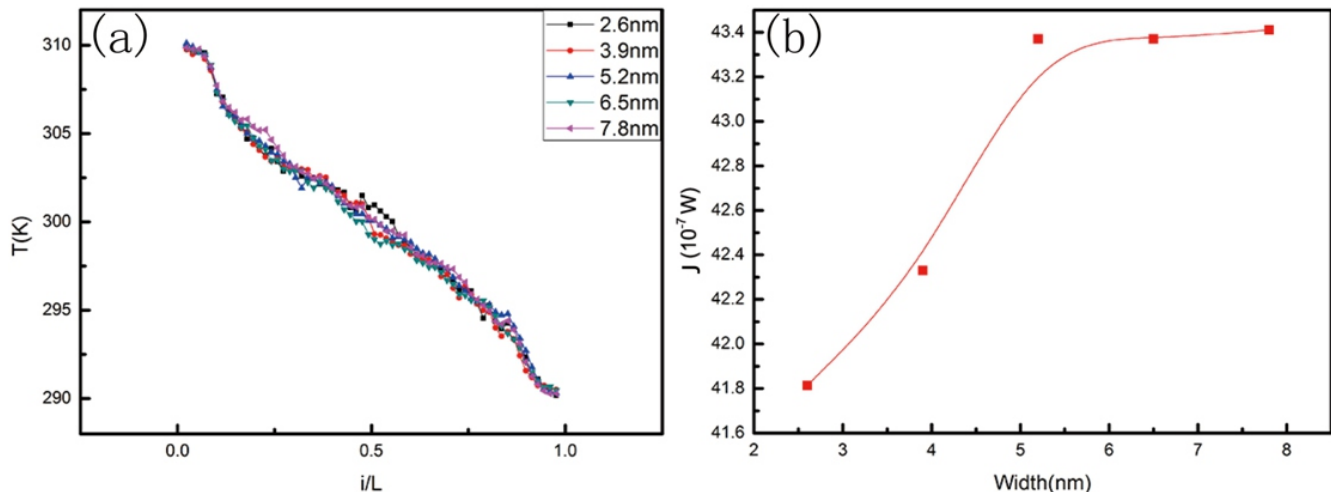


Fig. 5 Impacts of width on thermal properties of GFERS. (a) Temperature profile versus width. (b) κ versus width W from 2.6 nm to 7.8 nm. The other parameter $L = 17$ nm, $\bar{T} = 300$ K.

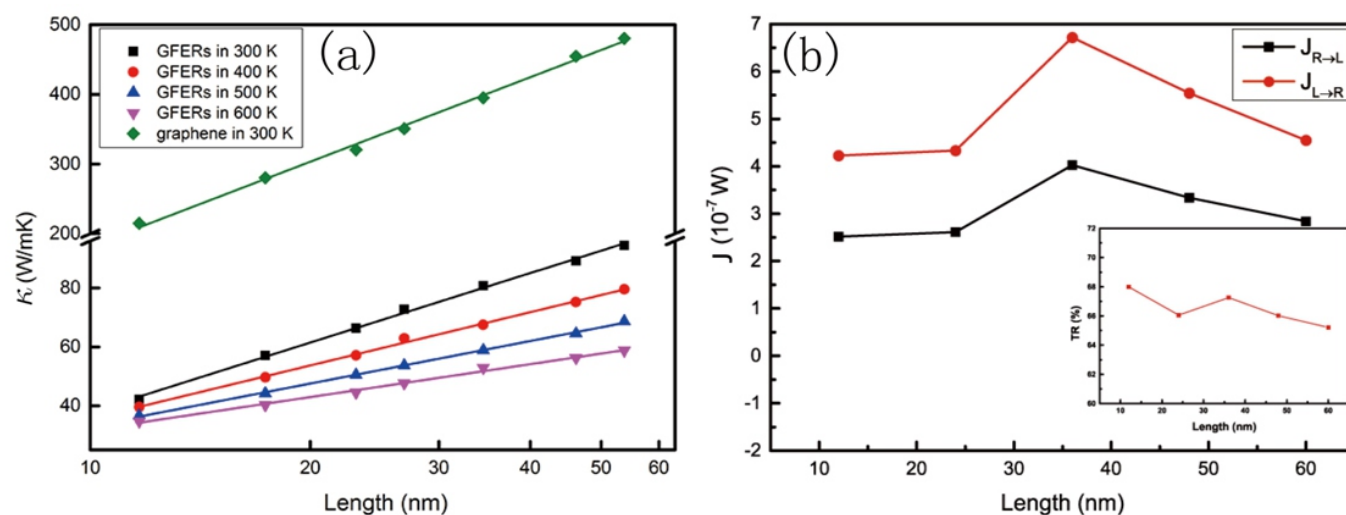


FIG. 6 (a) Impacts of length on thermal properties of GFERs and pristine graphene. The length L increase from 12 nm to 54 nm. The parameters are $W = 5.2$ nm, $\bar{T} = 300$ K for pristine graphene and increases from 300 K to 600 K for GFERs. The thermal conductivity κ versus the length L in log scale. (b) The heat flux versus the length of the graphene-GFERs heterostructure system. The thermal rectification ratio versus the length is shown in insets.

simulation shows that the thermal conductivity increases with L as $\kappa \propto \log L$.⁴²⁻⁴⁴ Here, L is changed from 12 nm to 54 nm at different temperatures. The κ increases from 42.1 W/mK to 92.5 W/mK at 300 K. Results at other temperatures (300 K to 1000 K) are all shown in Fig. 6(a). It exhibits the same behavior as pristine graphene, which has been found in experimental study.⁴² It can be seen that, κ of GFERs is much smaller than that of pristine graphene. It has been verified that the thermal conductivity contributed by short-range acoustic and optical phonons is temperature independent in previous works.^{45,46} In graphene, the long-range acoustic phonons dominate the thermal transport.⁴⁷ The significant decrease of thermal conductivity of GFERs is probably caused by the affected long-range acoustic phonons due to change of the dispersion relation.²⁹

Fig. 6(b) shows the heat flux from two different directions versus the length in the graphene-GFERs heterostructure system, the red line

represents the heat flux along the pristine graphene to the GFERs direction, the black is the heat flux from opposite direction, and the insets is the TR ratio versus the system length. The average temperature \bar{T} is fixed as 300 K, the normalized temperature bias $\Delta = 0.3$, and change the length L from 12 nm to 60 nm, the result show that the thermal rectification decreases with the increasing of the system length, which due to the thermal transport transits to the diffusive regime.^{7,15} But when the length is more than 60 nm, the TR ratio still have 65%. This indicates that such a heterostructure is a very excellent thermal rectifier which can be suitable for a wide range of system length.

Then, it is discussed the temperature dependence of κ where the length is changed from 12 nm to 27 nm in Fig. 7(a). It is found that κ decrease with the average temperature increasing as T^{-1} ,⁴⁸ due to the Umklapp phonon-phonon scattering, graphene has a T^{-1} behavior which is consistent with previous work.^{49,50} However, for GFERs, the values of

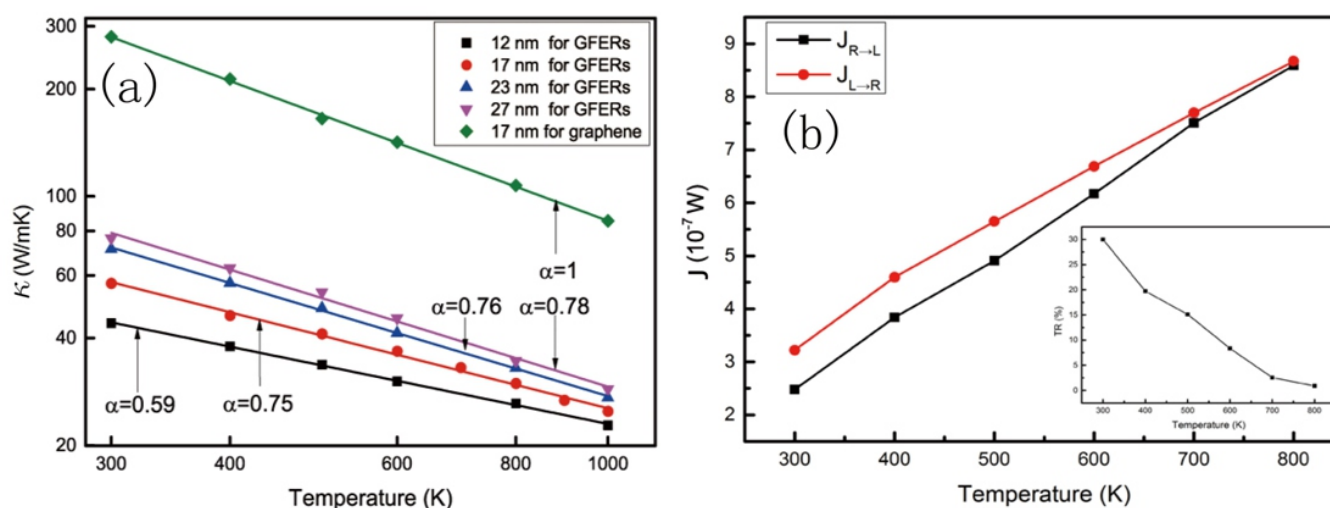


Fig. 7 (a) Thermal conductivity of GFERs and pristine graphene with different average temperature \bar{T} . The \bar{T} increases from 300 K to 1000 K. The parameters are $W = 5.2$ nm, the length L is 17 nm for graphene and increase from 12 nm to 27 nm for GFERs. The figure is plotted in a log-log scale. The symbols are numerical data and the lines are fitted lines. (b) The heat flux versus the average temperature \bar{T} of the graphene-GFERs heterostructure system, and the thermal rectification ratio versus \bar{T} is shown in insets.

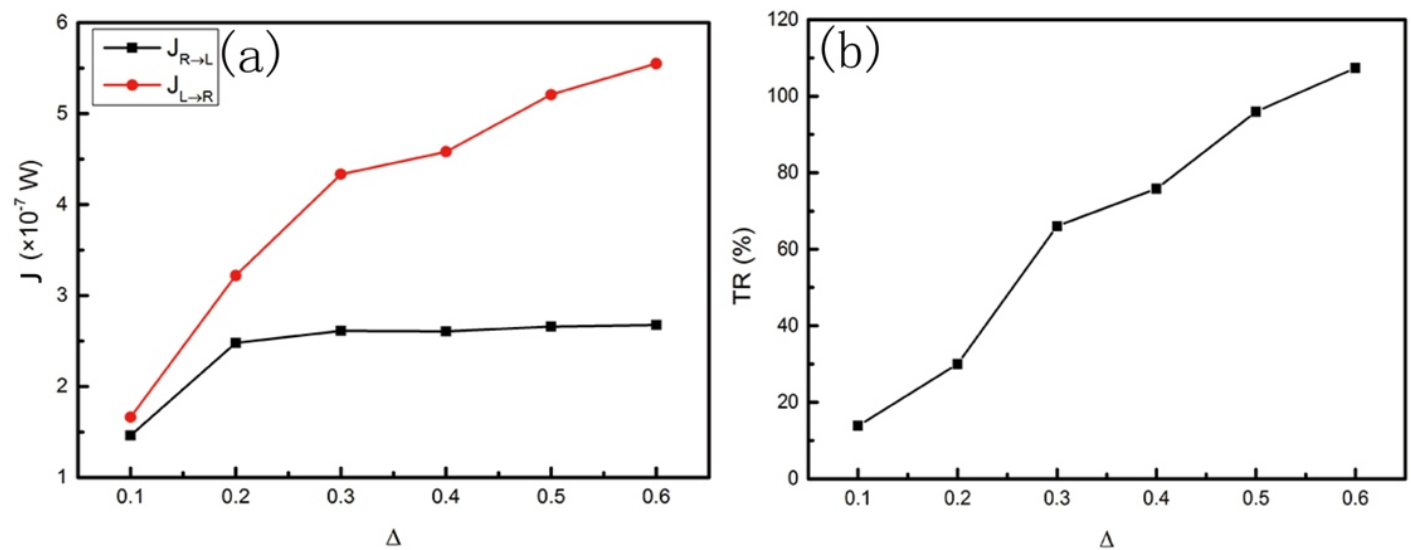


Fig. 8 The dependence of the normalized temperature bias Δ of the graphene-GFRs heterostructure system on the thermal rectification. (a) The heat flux versus normalized temperature bias Δ , the red line represents the heat flux along the pristine graphene to the GFRs direction, and the black line represents the heat flux from the opposite direction. (b) The thermal rectification ratio versus Δ .

α are 0.59, 0.75, 0.76 and 0.78. Obviously, the power exponents (α) increases with increasing the length.⁵¹ Thus, it is expected that α approaches 1 with increase of the length.

It is also discussed that the temperature dependence of the TR ratio in the graphene-GFRs heterostructure system. L is 48 nm, Δ is 0.2, and the average temperature \bar{T} changes from 300 K to 800 K. From Fig. 7(b) it can be found that with the \bar{T} increasing, the heat flux along two directions both increases, but the growth rate of the heat flux along the pristine graphene to the GFRs direction is smaller than that in the opposite direction. As a result, the calculated TR ratio decreases with the \bar{T} increasing. The largest TR ratio is 30% in 300 K, but only 1% in 800 K. It is because that thermal rectification is mainly caused by the mismatch of the phonon spectrum on both sides of the rectifier, but increasing the average temperature can weaken this mismatch effect, hence the TR ratio is restrained.⁵⁹

In the following, a discussion on the mechanism of rectification in graphene-GFRs heterostructure system is made based on the difference between thermal resistance of two directions, $(T_L - T_R)/J_{L \rightarrow R}$ and $(T_R - T_L)/J_{R \rightarrow L}$, which has a reciprocal relationship with the thermal conductivity. As shown in Fig. 7(a), the resistances of GFRs are more than three times larger than those of graphene. So, the resistances of GFRs dominates in the total resistance of heterostructure. The resistances depend on the temperature. The difference between two directions total resistance originate mainly from the resistance of GFRs at different temperatures. When the heat transfers from GFRs to graphene, the GFRs region has a higher temperature, corresponding to a lower heat flux and higher resistance. For the inverse direction, from graphene to GFRs, the GFRs region has a lower temperature, corresponding to a higher heat flux and lower resistance. It means the heat flux preferring from GFRs to graphene. This is different from the situation in graphene-graphene phononic crystal system,¹³ because the resistance of graphene phononic crystal is independent on the temperature and the resistance of graphene dominates in the total resistance of graphene-graphene phononic crystal system.

Finally, the dependence of the normalized temperature bias Δ of the graphene-GFRs heterostructure system on the thermal rectification is studied. The average temperature \bar{T} is fixed as 300 K, the system length

L is 48 nm, and the Δ changes from 0.1 to 0.6. Fig. 8(a) is the heat flux along two directions versus the Δ , it can be seen that with the increasing of the Δ , the heat flux along the pristine graphene to the GFRs direction increases steadily, while the heat flux from the opposite direction increases firstly but then becomes stable. Thus the TR ratio increases with the increasing of the Δ .⁵² From Figure 8(b) it can be seen that, when the $\Delta=0.6$, the TR ratio is up to 100%, which exceeds many other graphene based thermal rectifiers.⁵⁷ It indicates that this asymmetric structure is a good thermal rectifier which have a great potential in the field of thermal management.

4. Conclusions

In conclusion, it has been calculated the lattice thermal conductivity of graphene periodically embedded with four- and eight-membered rings as realized in recent experiment, and the thermal rectification of the graphene-GFRs asymmetric structure. It is found that, the length and temperature dependence of the thermal conductivity follow similar trends as the pristine graphene structure. But the magnitude of the thermal conductivity drops by several factors. This low thermal conductivity could be useful in thermoelectric and other applications, where reducing the thermal conductivity may help to increase the performance. It is also found that the heat flux along the pristine graphene to the GFRs direction is larger than that in opposite direction, and the smaller system length, lower average temperature, and higher temperature bias is the optimal condition to obtain the higher TR ratio.

Acknowledgments

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